

# Mathematical Model for Predicting Thrust Force in Drilling of GFRP Composites by Multifaceted Drill

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# Abstract

In this work an attempt has been made to develop empirical relationships to model thrust force in drilling of GFRP composites by Multifaceted drill bit. The empirical relationships were developed by response surface methodology incorporating above drilling parameters. The developed model can be effectively used to predict the thrust force in drilling of GFRP composites within the factors and their limits are studied.

**Keywords:** Drilling, GFR-polyester Composites, Modelling, Thrust Force, Optimisation.

# 1. Introduction

In recent years, Glass Fiber Reinforced Plastic composites (GFRP) have been extensively used in variety of engineering applications varying from aerospace to automobile industries. GFRP possess high strength and stiffness, ease of molding complex shapes, high corrosion resistance which make the material superior to metals for many applications. GFRP composite components are commonly fabricated by filament winding, hand lay-up, resin transfer moulding process. After fabrication, they require further machining for structural assemblies.

In drilling of GFRP composites, thrust force is the important criteria and the most effective way of achieving quality holes while drilling fiber reinforced plastics is by reducing the thrust. The effect of thrust force on drilling of GFRP composites is studied by many researchers. Davim et al. [1] carried out a study on milling of Glass fiber reinforced plastic composites manufactured by hand lay-up process. They used two types of GFRP composites to evaluate the cutting parameters such as cutting velocity and tool feed rate. Murphy et al. [2] studied the Thrust forces with respect to the drill bit and the work piece being drilled. They found out that the maximum thrust force was observed during a test run when the tool reaches the bottom of the laminate. Engin et al. [3] studied the orthogonal cutting mechanisms of Medium density fibre by developing the models of mechanics of orthogonal cutting. When GFRP composites are drilled, one should concentrate on the machining and friction force acting on it. Abrao et al. [4] investigated the effect of cutting tool geometry and material on thrust force and delamination produced while drilling GFRP composites. The major problem encountered during drilling of GFRP composites is delamination, which is occurred due to the thrust force developed during machining. Latha and Senthilkumar [5] studied delamination in drilling of GFR composites. They used 3 different types of K10 carbide tools to conduct experiments. Khashaba

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Fiber/resin	Tensile modulus Tensile strength		Density (a) (a/cm <sup>3</sup> )	Shear	Ultimate	
	(E) (GPa)	(σ) (MPa)	Density (p) (g/cm)	modulus	elongation (%)	
E-Glass	69	2400	2.6	27	-	
Polyester	3000	50	1.10	-	2%	

Table 1.Properties of fiber and resin



**Figure 1.** Close-up view of vertical machining centre (VMC100).

et al. [6] have studied the influence of material variables on thrust force, torque and delamination while drilling of GFRP composites. They have carried out the experiment with cross winding /polyester, continuous winding /polyester, woven polyester and woven /epoxy. They concluded that woven /epoxy combination posses better performance over others. Claudin et al. [7] conducted drilling experiments to determine suitable cutting tool for machining a low carbon steel using using different drill bits such as solid carbide drills, solid carbide modular drills, and indexable drills. They modeled axial force and cutting torque as a function of diameter, rake angle, cutting velocity, and feed rate and they found out the methodology to determine the drill geometry effect.

From the above literature, it has been known that the thrust force is an important concern and it has to be minimized. To get minimum thrust force, it is necessary to employ optimization techniques to find optimal cutting parameters and theoretical models to do predictions. Response Surface Methodology (RSM) is finding enormous applications in solving variety of complex engineering and scientific problems. Response Surface Methodology (RSM) is a collection of statistical and mathematical techniques useful for developing, improving, and optimizing processes. The most extensive applications of RSM are in the particular situations where several input variables potentially influence some performance measure or quality characteristic of the process [8]. Stone and Krishnamurthy [9] utilized a neural network thrust force controller to minimize delamination during drilling of graphite-epoxy laminates. Researchers successfully modeled and optimized by using a sequence of designed experiments to obtain an optimal response by knowing less about the process by using RSM [10-12]. Latha and Senthilkumar [13] have successfully applied fuzzy logic for the prediction of thrust force in drilling of GFRP composites. They used Pareto analysis of variance (Pareto-ANOVA) and analysis of variance (ANOVA) for analysis of machining parameters in drilling of GFRP composites. In the present study, effect of cutting parameters on thrust force on the drilling of GFRP composites by Multifaceted tool is evaluated and second order model is developed for predicting the thrust force. The predicted and measured values indicate that the developed model can be effectively used to predict the thrust force in the drilling of GFRP composites.

# 2. Materials and Method

The GFR-Polyester specimen used for this investigation is prepared by using hand lay-up technique. Unsaturated polyester resin matrix reinforced with 60% weight E - glass fiber is used for preparation and the thickness of the material is approximately 10 mm. The density of the polymer used is 1.10 g/cm<sup>3</sup>. The resin used for the fabrication of composite material is polyester and the hardner used is methyl ethyl ketone peroxide and accelerator is Kerox C-20. The specimen is having length 180 mm, breadth 90 mm, and height 12 mm. The properties of the fiber and resin are presented in Table 1.

The experiments were conducted in computer numeric control (CNC) vertical machining centre (VMC100). The machining center has a maximum spindle speed of 5000 rpm with a table size of 1270 x 254 mm and is presented in Figure 1. Multifaceted drill bits supplied from Woodtech USA were used for experimentation and are presented in Figure 2. Kistler piezo-electric dynamometer is used for capturing the thrust force obtained in drilling of GFRP composites, which is presented in Figure 3.



Figure 2. Multifaceted drills used for the experimentation.

**Table 2.** Specification of the dynamometer used forthe experiment

Туре	Calibrated 9257B
Weight	7.3 kg
Length*Width*Height	170 mm*100 mm*60 mm
Type of sensor	Piezoelectric
Number of channels	8
Multichannel amplifier-type	5019/5017
Operating temperature range, °C	0-70

The thrust force obtained can be measured using Multi channel amplifier type Dynamometer, whose specification is presented in Table 2 and the figure of the dynamometer is presented in Figure 3.

#### 2.1 Response Surface Methodology

RSM is a collection of mathematical and statistical techniques, which are useful for predicting the models and analyzing the problems in which more than one responses are influenced by several factors. The mathematical model of the response to independent controllable factors can be predicted, by using the multiple regression analysis with minimum number of experiments planned through design of experiments [14]. In our study, the second order polynomial models have been developed to predict the Thrust force, which is influenced by feed rate (f) and cutting speed (v), Drill diameter (d) and Fibre orientation angle ( $\theta$ ). The values of the regression coefficients of linear, quadratic and interaction terms of the mathematical models are determined by the following formula:

$$B = (X^{\mathsf{t}} X)^{-1} X^{\mathsf{t}} Y \tag{1}$$

where, B is the matrix of parameter estimates, X is the calculation matrix includes linear, quadratic and interaction terms, X <sup>t</sup> is the transpose of X and Y is the matrix of response.



Figure 3. Close-up view of Dynamometer.

Statistical design of experiments is used for experimentation. Due to the wider ranges of parameters selected, it has been decided to use five levels, central composite, rotatable design. Central composite rotatable design of second order was found to be the most efficient tool in response surface methodology to establish the mathematical relation of the response surface using the least possible number of experiments without losing its accuracy [15]. From the literature [2–5] and the previous work conducted in this field by authors [16,17], the independently controllable predominant drilling parameters which affect the Thrust force during the drilling of GFRP composite work piece have been identified. They are spindle speed (N), feed rate (f), Drill diameter (d) and fiber orientation angle ( $\theta$ ). Table 3 presents the ranges of factors considered and Table 4 shows the 30 sets of coded conditions used to form the design matrix, the parameters used, real values and output response.

The first 16 experimental conditions are derived from half factorial experimental design matrix  $(2^4=16)$ . All the variables at the intermediate (0) level constitute the center points while the combinations of each process variable at either its lowest (-2) or its highest (+2) with the other 8 variables of the intermediate levels constitute the star points. Thus, the 30experimental conditions allowed the estimation of the linear, quadratic and twoway interactive effects of the variables on the thrust force in drilling of GFRP composites.. For the convenience of recording and processing of the experimental data, upper and lower levels of the factors are coded as +2 and -2, respectively [18].

Cutting	Symbol	Unit	Range	Level 1	Level 2	Level 3	Level 4	Level 5
Parameters								
Spindle Speed	Ν	rev/min	500-2000	500	875	1250	1625	2000
Feed rate	f	mm/min	50-300	50	112.5	175	237.5	300
Drill Diameter	d	mm	4–12	4	6	8	10	12
Fiber orientation angle	θ	degrees	0–90	0	22.5	45	67.5	90

 Table 3.
 Control factors and level used for experimentation

Table 4. The parameters used, their coded values, real values and output response

Input parameters							Output		
	Coded Value Real Value						Response		
Exp. No	Spindle Speed (rpm)	Tool Feed rate (mm/min)	Drill diameter (mm)	Fiber orientation angle, degrees	Spindle Speed (rpm)	Tool Feed rate (mm/ min)	Drill diameter (mm)	Fiber orientation angle, degrees	Thrust force
1	-1	-1	-1	-1	875	112.5	6	22.5	119.61
2	1	-1	-1	-1	1625	112.5	6	22.5	102.45
3	-1	1	-1	-1	875	237.5	6	22.5	175.78
4	1	1	-1	-1	1625	237.5	6	22.5	142.41
5	-1	_1	1	-1	875	112.5	10	22.5	142.41
5	-1	-1	1	-1	1625	112.5	10	22.5	109.79
7	-1	-1	1	-1	875	237.5	10	22.5	275 72
8	-1	1	1	-1	1625	237.5	10	22.5	183.12
9	-1	-1	-1	1	875	112.5	6	67.5	114.62
10	1	-1	-1	1	1625	112.5	6	67.5	112.26
11	-1	1	-1	1	875	237.5	6	67.5	186.58
12	1	1	-1	1	1625	237.5	6	67.5	141.95
13	-1	-1	1	1	875	112.5	10	67.5	169.25
14	1	-1	1	1	1625	112.5	10	67.5	117.95
15	-1	1	1	1	875	237.5	10	67.5	272.29
16	1	1	1	1	1625	237.5	10	67.5	175.12
17	-2	0	0	0	500	175	8	45	203.62
18	2	0	0	0	2000	175	8	45	96.12
19	0	-2	0	0	1250	50	8	45	85.26
20	0	2	0	0	1250	300	8	45	230.51
21	0	0	-2	0	1250	175	4	45	92.79
22	0	0	2	0	1250	175	12	45	207.16
23	0	0	0	-2	1250	175	8	0	148.95
24	0	0	0	2	1250	175	8	90	163.78
25	0	0	0	0	1250	175	8	45	272.63
26	0	0	0	0	1250	175	8	45	266.56
27	0	0	0	0	1250	175	8	45	256.51
28	0	0	0	0	1250	175	8	45	280.61
29	0	0	0	0	1250	175	8	45	269.82
30	0	0	0	0	1250	175	8	45	235.86

The coded value of any intermediate levels can be calculated by using the following expression [18, 19].

$$X_{i} = \frac{\left[2X - (X_{max} + X_{min})\right]}{\left[\frac{X_{max} - X_{min}}{2}\right]}$$
(2)

where,  $X_{\text{max}}$  is the upper level of the parameter,  $X_{\text{min}}$  is the lower level of the parameter and  $X_{\text{i}}$  is the required coded values of the parameter of any value of X from  $X_{\text{min}}$  to  $X_{\text{max}}$ .

The experiments are conducted as per the formulated design, and the images of the hole recorded at different conditions were presented in Table 5.

#### 2.2 Modeling of Drilling Parameters using RSM

The second order response surface equations for the Thrust force (Fz) in drilling of GFRP composites can be expressed as:

$$Fz = f(v, f, d, \theta)$$
(3)

The general quadratic response-surface model, used to evaluate the parametric effects is as follows:

$$Y = b_0 + \Sigma bi xi + \Sigma bii xi^2 + \Sigma bij xi xj$$
(4)

where  $b_0$  is the coefficient for constant term and *bi*, *bii*, *bij* are the coefficients for linear, square and interaction terms respectively.

The model chosen was a second degree response surface expressed as follows:

$$F_{d} = \beta_{0} + \beta_{1}(v) + \beta_{2}(f) + \beta_{3}(d) + \beta_{4}(\theta) + \beta_{5}(v^{2}) + \beta_{6}(f^{2}) + \beta_{6$$



Figure 4. Normal probability plot.

 $\beta_{7}(d^{2}) + \beta_{8}(\theta^{2}) + \beta_{9}(vf) + \beta_{10}(vd) + \beta_{11}(v\theta) + \beta_{12}(fd) + \beta_{13}(f\theta) + \beta_{14}(d\theta).$ (5)

The model developed based on the above is given below:

Thrust force =  $263.66500 - 24.35292^*\nu + 33.30125^*f + 26.46792^*d + 0.49542^*\theta - 10.37938^*\nu^2 - 10.90188^*f^2 - 1.34063^*d^2 + 7.03562^*\theta^2 + 0.97437^*\nu^*f - 3.00563 V^*d - 26.98177 V^*\theta - 24.94052 f^*d - 26.95552f^*\theta - 25.35802 d^*\theta$  (6)

Analysis of variance (ANOVA) technique is used to check the adequacy of the developed empirical model and is presented in Table 6. The response of thrust force, the model F value of 9.86 implies that the model is significant. Values of "Prob>F" less than 0.0500 indicate that the model terms are significant. The calculated value of the F ratio of the developed model is less than the standard F ratio (from F table) value at a desired level of confidence (say 95%), then the model is said to be adequate within the confidence limit.

The "Predicted R-Squared" of 0.98 is in reasonable agreement with the "Adjusted R-Squared" value. The calculated value of the R ratio of the developed relationships exceeds the standard tabulated value of the R ratio for a desired level of confidence (say 95%), then the relationship may be considered to be adequate within the confidence limit and hence the model may be accepted. The experimental data and the predicted data by the using aforesaid model are analysed by using residual analysis. In this method, confidence interval and prediction interval could be close to each other and narrower intervals provide a higher degree of precision which is presented in Figure 4 and the predicted value versus the actual experimental value is presented in Figure 5 which shows better correlation.



**Figure 5.** Comparison plot for thrust force using Multifaceted drill bit.

8	0		0	
V=875, f=112.5, d=6, θ=22.5	V=1625, f=112.5, d=6, θ=22.5	V=875, f=237.5, d=6, θ =22.5	V=1625, f=237.5, d=6, θ =22.5	V=875, f=237.5, d=10, θ =22.5
6	0	0		
V=1625, d=112.5, d=10, θ=22.5	V=875, d=237.5, d=10, θ =22.5	V=1625, d=237.5, d=10, θ=22.5	V=875, d=112.5, d=6, θ=67.5	V=1625, d=112.5, d=6, θ=67.5
	-	-		
V=875, d=237.5, d=6, θ=67.5	V=1625, d=112.5, d=10, θ=22.5	V=875, d=112.5, d=10, θ=67.5	V=1625, d=112. 5, d=10, θ=67.5	V=875, d=237.5, d=10, θ=67.5
V=1625, d=237.5, d=10, θ=67.5	V=500, d=175, d=8, θ=45	V=2000, d=175, d=8, θ=45	V=1250, d=50, d=8, θ=45	V=1250, d=300, d=8, θ=45
V=1250, d=175, d=4, θ=45	V=1250, d=175, d=12, θ=45	V=1250, d=175, d=8, θ=0	V=1250, d=175, d=8, θ=90	V=1250, d=175, d=8, θ=45
				0
V=1250, d=175, d=8, θ=45	V=1250, d=175, d=8, θ=45	V=1250, d=175, d=8, θ=45	V=1250, d=175, d=8, θ=45	V=1250, d=175, d=8, θ=45

 Table 5.
 Record of hole quality using Multifaceted Drill

Table 6.	Analysis	of variance	for r	esponse	surface
regression	model				

Source	DF	Seq SS	Adj SS	Adj MS	F	Р
Regression	14	114505	114505	8178.9	52.45	0.000
Linear	4	57628	57628	14407.0	92.39	0.000
Square	4	52271	52271	13067.8	83.81	0.000
Interaction	6	4606	4606	767.6	4.92	0.006
Residual Error	15	2339	2339	155.9		
Total	29	116844				
R-Sq = 98.00%						

### 3. Results and Discussions

GFRP composites finds increased application of in many engineering fields ranging from automotive to aeronautical industries. Drilling is an un avoidable process in manufacturing, since parts cannot be made near net-shape. During drilling of GFRP composites, many problems encountered including defuzzing, spalling, delamination, fiber-pull out etc. Among these problems, delamination due to thrust force causes severe damage to the product, which leads to the rejection of material. The industrial engineers spending effort to minimize the thrust force which in turn produce delamination. The experts may easily analyse the damages occurred in drilling of GFRP composites by the picture taken from Scanning electron microscope. The surface profiles obtained and the enlarged view of the profile observed in drilling of GFRP composites are presented in Figure 6a and 6b respectively.

In Figure 6a, there is a smooth surface observed in some region of the specimen, whereas some region does not show clear effect on the work surface. This may be due to the interrupted cutting takes place due to the multiedge drill tool used for this purpose. Figure 6b shows the SEM microstructure of the specimen observed. The result indicated that there is a insufficient distribution of resin and fibre in the cut surface. During the cutting process, there is a small variation in surfaces observed, which is indicated in the figure.

#### 3.1 Effect of Drilling Parameters on Thrust Force

GFRP drilling is complicated comparing to machining of metals and alloy due to its anisotropic nature. Proper care

should be taken to select the range of parameters. The effect of different parameters such as spindle speed, feed rate, drill diameter and fiber orientation angle in drilling GFRP composites have been discussed in detail in the following paragraph.

Figure 7(a-f) shows the interaction effect of the parameter on the drilling of GFRP composites. The effect between the parameter spindle speed and feed rate is presented in Figure 7a. The figure indicated that the increase of feed rate increases the thrust force in drilling of GFRP composites. The reason being the increase of feed rate increases the load on the tool, which resulted in increase of thrust force.

Figure 7b shows the effect of spindle speed and drill diameter versus the thrust force in drilling of GFRP composites. The result indicate that the increase of drill diameter increase the contact area between the drill and workpiece which resulted in high thrust force, whereas the increase of spindle speed does not show any clear trend as observed before. Figure 7c shows the effect of feed rate and drill diameter on thrust force in drilling of GFRP composites. The increase of drill diameter and feed rate increases the thrust force in drilling of GFRP composites as discussed earlier.

The effect of spindle speed and fiber orientation angle on thrust force in drilling of GFRP composites is shown in Figure 7d. The increase in the fiber orientation angle increase the thrust force upto 45°, after that the increase is not affected so much. The high thrust force is observed only at 45°. The spindle speed shows the same trend as discussed earlier. The effect of feed







Figure 6b. Enlarged view of the profile observed.



(e)Feed rate Vs Fiber orientation angle

(f)Drill diameter Vs Fiber orientation angle

Figure 7. (a,b,c,d,e and f) 3-D response graphs for Thrust force in drilling GFRP composites by using Multifaceted drill.

rate and fiber orientation angle with thrust force and the effect of drill diameter and fiber orientation angle with thrust force is presented in Figure 7e and 7f. The figure shows that the increase of feed rate and drill diameter increases the thrust force in drilling of GFRP composites, whereas 45° fiber orientation angle shows the maximum thrust force.

From the above figures it has been clearly seen that minimum feed rate, reasonably small drill diameter and  $0^{\circ}$  or  $90^{\circ}$  fiber orientation angle is preferred for

minimizing the thrust force in drilling of GFR-Polyester composites.

# 4. Conclusions

- The experiments are conducted as per Central composite design matrix using Multifaceted drill bit.
- The developed mathematical model can be effectively used to minimize thrust force in drilling GFRP composites.
- The results indicated that the effect of fiber orientation angle plays a major role in drilling GFRP composites.
- 0° or 90° fiber orientation angle is recommended for minimizing thrust force in drilling of GFRP composites.

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